

**TURKISH  
AVIATION  
ACADEMY**



**İTÜ**



*Estimation of Demand and Market Share*  
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*M.Sc. Program*

*Network, Fleet and Schedule*  
*Strategic Planning*  
*Module 7: 11 March 2014*

# *Lecture Outline*

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- **Air Travel Demand Models**
  - Time series vs. causal models for demand forecasting
  - Simple Market Demand Function
  - Demand Segmentation
  
- **Market Share Estimation**
  - Market Share vs. Frequency Share “S-Curve” Model
  - Quality of Service Index (QSI) Model
  - Logit Models of Passenger Choice

## *Air Travel Demand Models*

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- **Demand models are mathematical representations of the relationship between demand and explanatory variables:**
  - Based on our assumptions of what affects air travel demand
  - Can be linear (additive) models or non-linear (multiplicative)
  - Model specification reflects expectations of demand behavior (e.g., when prices rise, demand should decrease)
- **A properly estimated demand model allows airlines to better forecast demand in an O-D market:**
  - As a function of changes in average fares
  - Given recent or planned changes to frequency of service
  - To account for changes in market or economic conditions

## ***Demand Forecasting Methods***

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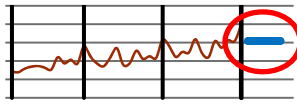
- **Time series methods extrapolate patterns in historical booking data to forecast demand**
  - Statistical methods to estimate recent growth/declines
  - Adjustment for known seasonality and cycles
- **Causal methods include additional explanatory variables that can affect future demand**
  - Actual advance booking data for future dates
  - Additional “exogenous” variables such as economic growth, expected changes in price or frequency
  - Adjustment for changes to competitive conditions

## Example: Combined Model for Estimating Total O-D Demand in a Market

### History Model

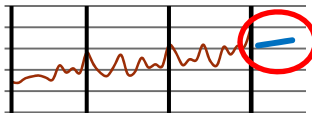
#### Step 1 Level

- Estimates the level of the industry using data\* of the previous year



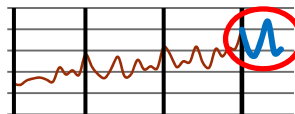
#### Step 2 Trend

- Estimates the trend of the industry using data of the two previous years



#### Step 3 Seasonality

- Estimates seasonality of the market using data of the three previous years



### Booking Model

#### Step 1 Indirect Bookings

- Compares MIDT bookings for the following months with the ones that existed for the same months of the previous year

#### Step 2 Total bookings

- Adds the estimations of direct bookings (Non MIDT)

#### Step 3 Estimation

- Uses the difference between last year bookings and last year actual traffic to estimate how much will the bookings increase

**By combining the results from the two models, the tool estimates the market size for the following 6 months**

## ***Simple Market Demand Function***

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- **Multiplicative model of demand for travel O-D per period:**

$$\mathbf{D = M \times P^a \times T^b}$$

where: M = market sizing parameter (constant) that represents underlying population and interaction between cities

P = average price of air travel

T = total trip time, reflecting changes in frequency

a,b = price and time elasticities of demand

- **We can estimate values of M, a, and b from historical data sample of D, P, and T for same market:**
  - Previous observations of demand levels (D) under different combinations of price (P) and total travel time (T)

## *Multiple Demand Segments*

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	<b>Business Air Travel Demand</b>	<b>Personal Air Travel Demand</b>
<b>First Class</b>	$D_{fb}$	$D_{fp}$
<b>Coach Class</b>	$D_{cb}$	$D_{cp}$
<b>Discount Class</b>	$D_{db}$	$D_{dp}$

## ***Demand Models by Segment***

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### **Demand Functions for Business Travel**

$$D_{fb} = M_b I_f P_f^{a1} T_f^{b1} P_c^{c1}$$

$$D_{cb} = M_b I_c P_c^{a1} T_c^{b1} P_f^{c1}$$

Where  $M_b$  = the market sizing parameter for business travel demand (constant)

$I_f, I_c$  = constant image factors for first and coach class services

$P_f, P_c$  = prices of first and coach class services

$T_f, T_c$  = total travel times for first and coach class services

$a1$  = price elasticity of demand for business travelers

$b1$  = time elasticity of demand for business travelers

$c1$  = cross-elasticity of business travel demand for first class service with respect to the price of coach class service, and vice versa



## ***Demand Models by Segment***

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### **Demand Functions for Personal Travel**

$$D_{cp} = M_p I_c P_c^{a2} T_c^{b2} P_d^{c2}$$

$$D_{dp} = M_p I_d P_d^{a2} T_d^{b2} P_c^{c2}$$

Where  $M_p$  = the market sizing parameter for personal travel demand (constant)

$I_c, I_d$  = constant image factors for coach and discount class services

$P_c, P_d$  = prices of coach and discount class services

$T_c, T_d$  = total travel times for coach and discount class services

$a2$  = price elasticity of demand for personal travelers

$b2$  = time elasticity of demand for personal travelers

$c2$  = cross-elasticity of personal travel demand for coach class service with respect to the price of discount class service, and vice versa

# *Issues in Price Elasticity Estimation*

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- **Sources of data**

- Airlines have detailed historical booking data by fare class
- US DOT 10% ticket sample provides flown ticket data for US domestic markets -- passengers and average fare by airline
- But, all available data reports traffic flown, *NOT* “demand”

- **Measurement issues**

- Ideally, need a dataset with no change to schedules, competitors, economic conditions
- Price and service attributes of travel substitutes (esp. short-haul)
- Cross-sectional, time series, or panel data samples
- Demand segmentation and revenue management impacts
- Identification problem – supply affects demand
- Focus on one airline (or airport) will exaggerate elasticity estimates

## ***Airline Competition***

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- **Airlines compete for passengers and market share based on:**
  - Frequency of service and departure schedule on each route served
  - Price charged, relative to other airlines, to the extent that regulation allows for price competition
  - Quality of service and products offered -- airport and in-flight service amenities and/or restrictions on discount fare products
- **Passengers choose among flight schedules, prices and product quality to minimize air travel disutility:**
  - Each passenger would like to have the best service on a flight that departs at the most convenient time, for the lowest price

## ***Market Share Estimation***

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- **Given estimate of total demand for air travel in an O-D market, what is each airline's market share?**
  
- **Several modeling approaches can be used to estimate airline market shares:**
  - “S-curve” model of market share/frequency share
  - Extensions to “Quality of Service Index” (QSI Model)
  - Logit Models used in profit estimation software systems

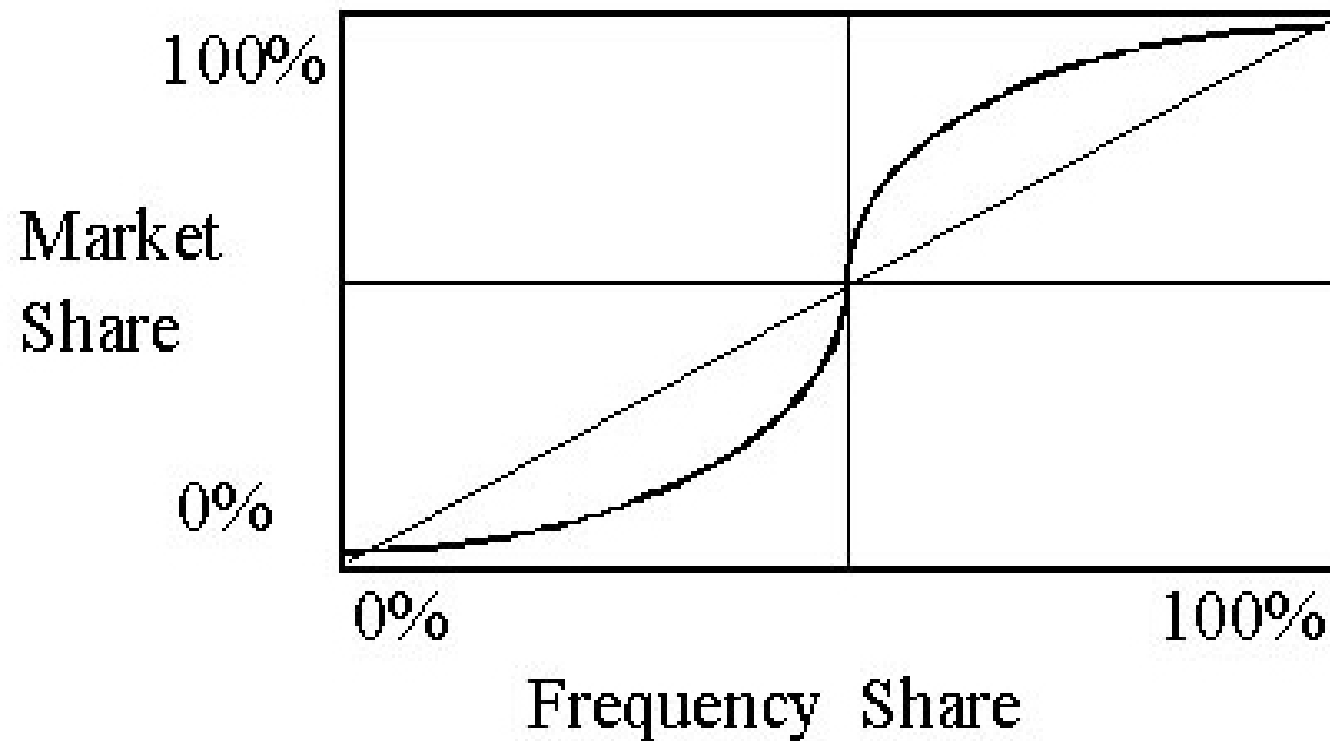
## ***Market Share / Frequency Share***

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- **Rule of Thumb**: With all else equal, airline market shares will approximately equal their frequency shares.
- **But there is much empirical evidence of an “S-curve” relationship as shown on the following slide:**
  - Higher frequency shares are associated with disproportionately higher market shares
  - An airline with more frequency captures all passengers wishing to fly during periods when only it offers a flight, and shares the demand wishing to depart at times when both airlines offer flights
  - Thus, there is a tendency for competing airlines to *match* flight frequencies in many non-stop markets, to retain market share

## *MS vs. FS “S-Curve” Model*

**Market Share vs Frequency Share “S-Curve” Model**



## *S-Curve Model Formulation*

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$$MS(A) = \frac{FS(A)^\alpha}{FS(A)^\alpha + FS(B)^\alpha + FS(C)^\alpha + \dots}$$

where  $MS(i)$  = market share of airline  $i$   
 $FS(i)$  = non-stop frequency share of airline  $i$   
 $\alpha$  = exponent greater than 1.0, and generally between 1.3 and 1.7

## ***Example: S-Curve Market Share Model***

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- **Single O-D market, short-haul non-stop route**
  - Two airlines, each offer 4 daily flights with 120 seat aircraft
  - Assume prices and service quality are equal
- **Total daily demand (PDEW) is a function of frequency**

$$\text{PDEW} = 10000 * [4 + 4 / \text{TOT FREQ}]^{-1.7}$$

- **S-curve model of MS vs. FS with alpha = 1.5**

	<u><b>AIRLINE A</b></u>	<u><b>AIRLINE B</b></u>
AIRCRAFT CAPACITY	120	120
TOTAL DAILY PAX	775	
FLIGHTS per day	4	4
FREQUENCY SHARE	50.0%	50.0%
MARKET SHARE	50.0%	50.0%
AIRLINE PAX PER DAY	387.7	387.7
AVE. LOAD FACTOR	80.77%	80.77%



## *Airline A Adds 1 New Flight*

- **Airline A expands its schedule to gain market share**

	<u>AIRLINE A</u>	<u>AIRLINE B</u>
AIRCRAFT CAPACITY	120	120
TOTAL DAILY PAX	792	
FLIGHTS per day	5	4
FREQUENCY SHARE	55.6%	44.4%
MARKET SHARE	58.3%	41.7%
AIRLINE PAX PER DAY	461.6	330.3
AVE. LOAD FACTOR	76.94%	68.82%

- **Airline A gains passengers and market share**
  - But its load factor decreases
  - Note that load factor of Airline B decreases even more!
  - If we assume both airlines have a **75% Break-Even Load Factor**, then Airline A's change causes Airline B to become unprofitable

## ***Discussion:*** ***How Should Airline B Respond?***

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- **What should Airline B do to regain profitability?**
  - Without changes to price, image, service quality
  - Schedule and capacity changes only

	<b><u>AIRLINE A</u></b>	<b><u>AIRLINE B</u></b>
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TOTAL DAILY PAX	792	
FLIGHTS per day	5	4
FREQUENCY SHARE	55.6%	44.4%
MARKET SHARE	58.3%	41.7%
AIRLINE PAX PER DAY	461.6	330.3
AVE. LOAD FACTOR	76.94%	68.82%

## *QSI Market Share Models*

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- **Quality of Service Index (QSI)**
  - Values an airline's set of flights offered in an O-D market, relative to competitors
  - Extension of simple MS/FS model to include one-stop and connecting flight options
  - Used to estimate the markets share potential of new routes and incremental flights
- **Developed in the 1960s, widely used by airlines for planning and scheduling**

## ***QSI Market Share Example***

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- **QSI for Buenos Aires (EZE) to Bogota (BOG)**

	<u>Number</u>	<u>Weight</u>	<u>Index</u>
Daily Nonstops	1	1.0	1.00
One-stop Flights	2	0.33	0.66
<u>Connections</u>	<u>8</u>	<u>0.03</u>	<u>0.24</u>
Market QSI			1.90

- **Current share of 1 non-stop flight =  $1.0/1.9 = 53\%$**
- **Impact on QSI of additional non-stop flight = 1.0**
- **New Market QSI is 2.90**

## ***Impacts of Adding a Second Non-stop Flight***

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- **Total demand EZE-BOG estimated as 250 PDEW**
  - (Assume new frequency stimulates demand by 10%)
- **QSI share for new non-stop flight**
  - =  $250 \times (1/2.90) = 250 \times 0.345 = 86$  passengers/day
- **Impacts on existing non-stop flight**
  - Previous share  $227 \times (1/1.90) = 227 \times 0.53 = 120$  pax
  - New share  $250 \times (1/2.90) = 86$  pax/day
- **Overall effect of adding a 2<sup>nd</sup> non-stop flight**
  - Increase in total pax from 120 to  $2 \times 86 = 172$ /day
  - Decrease in loads per flight from 120 to 86 = - 34

## ***Logit Models for Market Share Estimation***

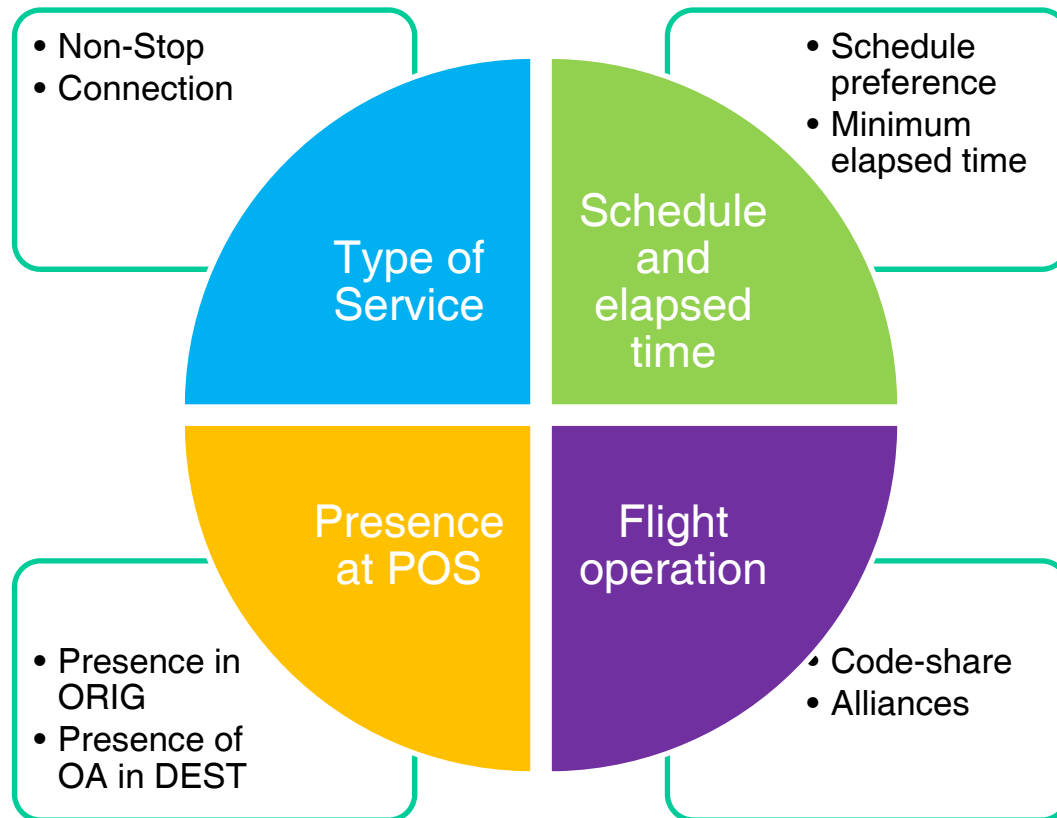
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- **“Discrete choice” models use logit formulation to further extend QSI approach**
  - Probability of passenger choice based on relative utilities of different flights/airlines in an O-D market
- **Utilities of flight alternatives can include:**
  - Path quality index (non-stop, 1-stop, connection) and/or actual elapsed trip times
  - Airline service quality and passenger preferences
  - Possible fare differences, frequent flyer programs, etc.
- **Historical input data needed to calibrate choice parameters**

# Logit Model Market Share Estimation

## Most important factors for passenger preference

## Mathematical Expression



$$MS(i) = \sum_{t=0}^{167} p(t) \frac{e^{\sum_J \beta_J x_J^i}}{\sum_{k=1}^m e^{\sum_J \beta_J x_J^k}}$$

***MS(i)*** is the market share of the itinerary *i* under consideration

***p(t)*** is the probability of a passenger requesting a departure hour *t* (TOW)

**$\beta_J = \beta_1, \beta_2, \dots, \beta_n$**  are the logit coefficients for each attribute

**$X_j^i = X_j^1, X_j^2, \dots, X_j^n$**  are the attribute variables for itinerary *i* as described in the previous section

**$k = 1, 2, \dots, m$**  are all the itineraries in the market

Source: LAN Airlines (2012)

# Logit Passenger Choice Model: New IST-BOS Non-stop Flight

- Estimate the probability of passenger choice for all flight paths in an OD city-pair
- Relative utility of different flights and paths based on trip duration and number of stops

